Embeddings of Weighted Tensor Product Spaces

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We study embeddings between tensor products of weighted reproducing kernel Hilbert spaces. The setting is based on a sequence of weights $\gamma_j > 0$ and sequences $1 + \gamma_j k$ and $1 + l\gamma_j$ of reproducing kernels k such that $H(1 + \gamma_j k) = H(1 + l\gamma_j)$, in particular. We derive necessary and sufficient conditions for the norms on $\bigotimes_{j=1}^s H(1 + \gamma_j k)$ and $\bigotimes_{j=1}^s H(1 + l\gamma_j)$ to be equivalent uniformly in s. Furthermore, we study relaxed versions of uniform equivalence by modifying the sequence of weights, e.g., by constant factors, and by analyzing embeddings of the respective spaces. Likewise, we analyze the limiting case $s = \infty$

This is joint work with Klaus Ritter.